Une théorie locale des polylogarithmes

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Extending the Eulerian functions, we study their relationship with zeta function of several variables. In particular, starting with Weierstrass factorization theorem (and Newton-Girard identity) for the complex Gamma function, and therefore we get a calculus on new entire functions. To this end, in order to index harmonic sums with computable series, we need to unfold a local theory of polylogarithms and their Taylor expansions at zero.

References

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